



# USING CAUSAL DISCOVERY ALGORITHMS TO ANALYZE AND PREDICT THE STRATOSPHERIC POLAR VORTEX

Marlene Kretschmer, 21.9.2017

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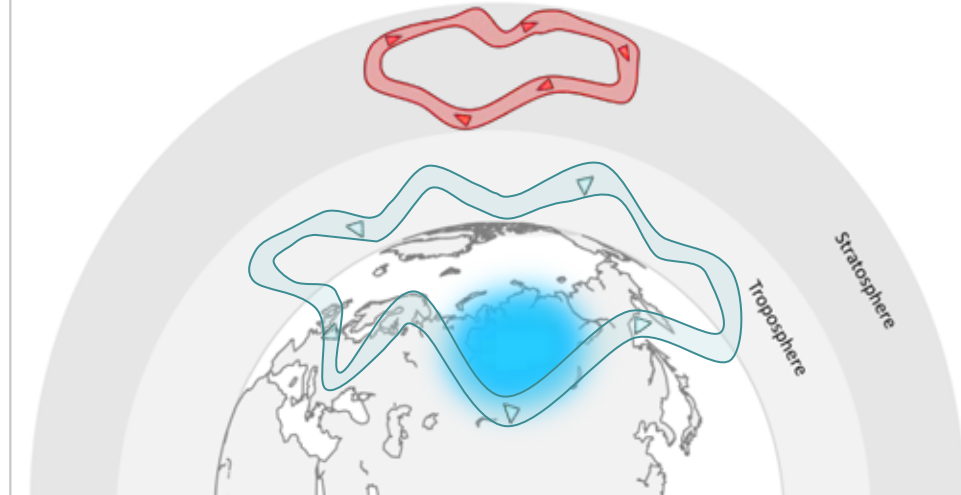
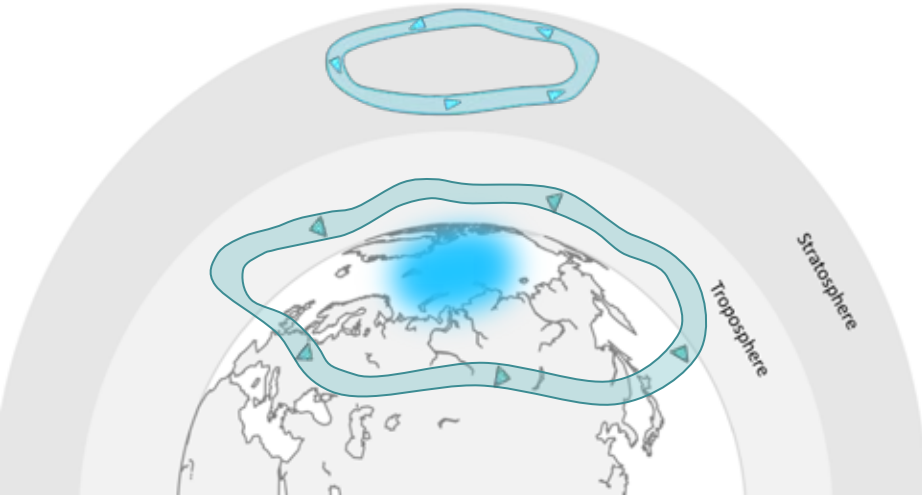
# THE STRATOSPHERIC POLAR VORTEX

Strong Polar Vortex:

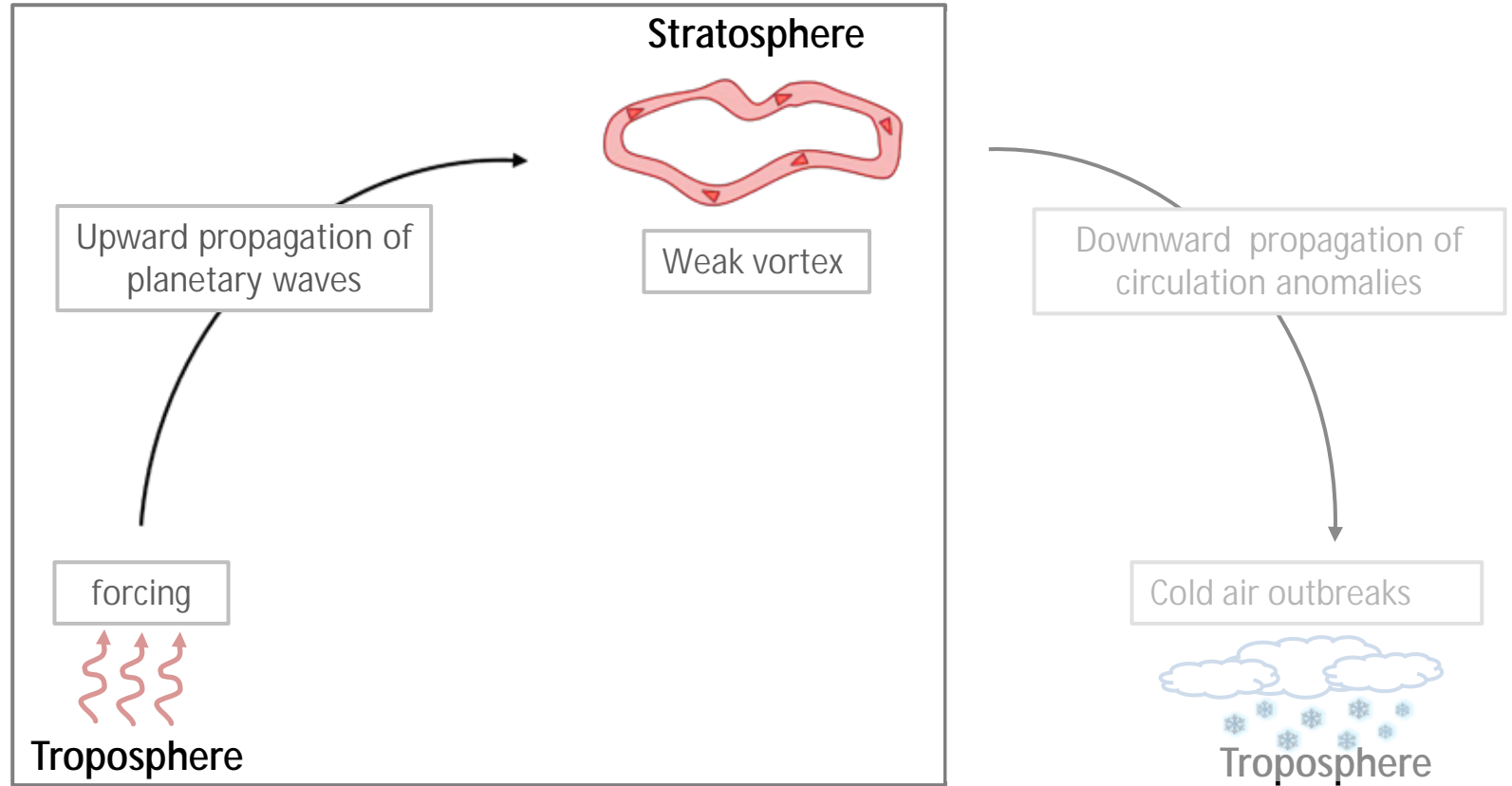
- Fast winds
- Strong, circumpolar flow
- à Mild winters/+AO

Weak Polar Vortex:

- Slow winds
- Weak, wavy flow
- à Cold winters/-AO



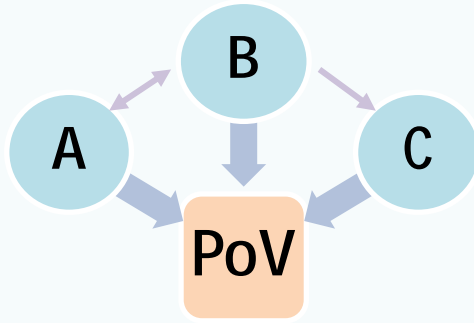
# TROPOSPHERE - STRATOSPHERE - TROPOSPHERE COUPLING



# OUTLOOK

## PART I

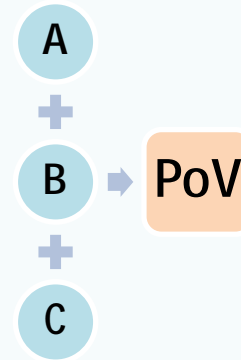
Causal effect networks for hypothesis testing



(Arctic) drivers of the polar vortex

## PART II

Response-guided causal precursor detection for predictions

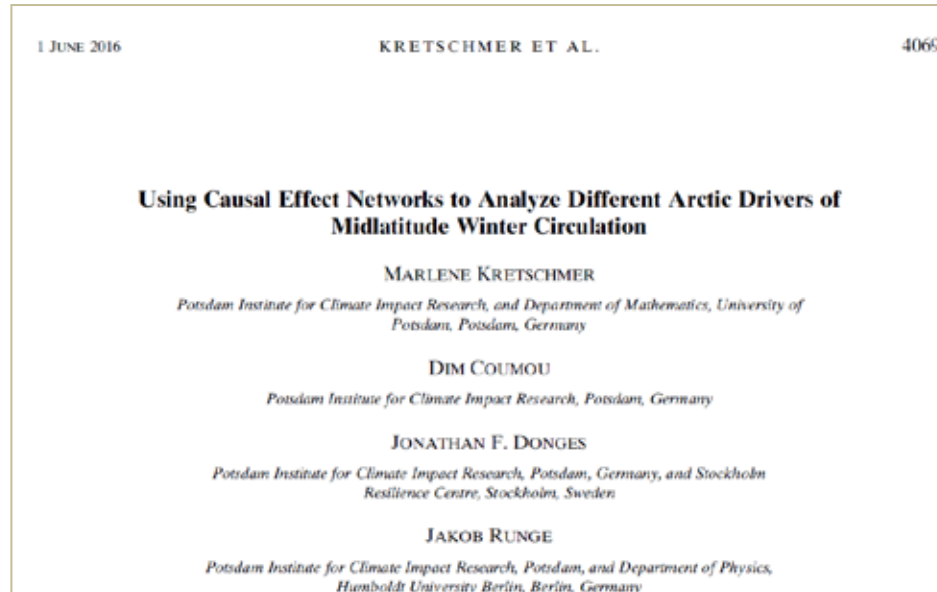


Predict polar vortex variability

Common tasks when studying teleconnections

# PART I

## Hypothesis testing with Causal Effect Networks



# HYPOTHESIS: ARCTIC DRIVERS OF POLAR VORTEX VARIABILITY

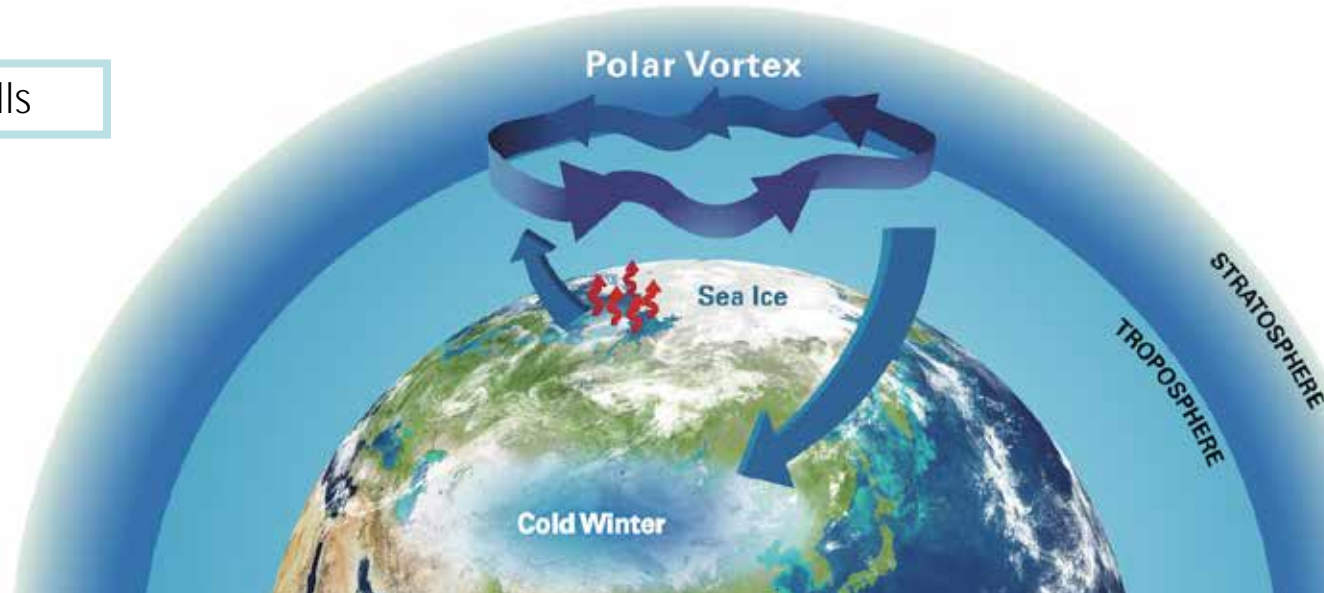
Low sea-ice concentrations in fall in the Barents-Kara Seas  
(e.g. Kim et al, *Nat Comm*, 2014)



Enhanced snow cover in fall  
(e.g. Cohen et al, *J Clim*, 2014)

lead to higher surface pressures, upward wave propagation, weakening of polar vortex

favor -AO and mid-lat cold spells



## DATA SELECTION: CHOOSE VARIABLES FOR EACH "ACTOR"

Abbreviation	Actor	Variable/Unit	Region (Level)
BK-SIC	Barents Kara sea ice	Sea ice area fraction	70 °- 80°N, 30°- 105°E
EA-snow	Eurasia snow cover	snow covered area fraction	40° - 80°N, 30°-180°E
Sib-SLP	Siberian High	Sea level pressure	40° - 65°N, 85° - 120°E
Ural-SLP	Ural Mountains sea level pressure	Sea level pressure	45° - 70°N, 40° - 85°E
v-flux	Vertical wave propagation	Pole-ward eddy heat flux $v^*T^*$	45° - 75°N (100 mb)
PoV	Polar Vortex	Geopotential height in m	65° - 90°N (10 - 100 mb)
AO	Arctic Oscillation Index	Geopotential height	20° - 90°N (1000 mb)

PoV



AO



BK-SIC



EA-snow



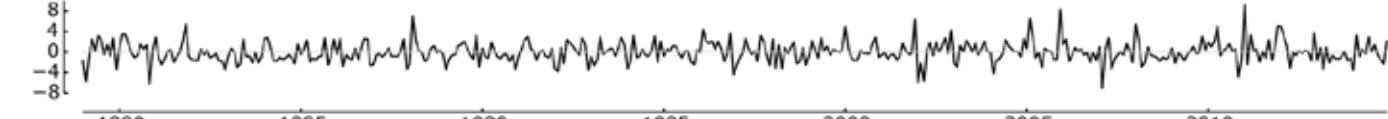
vflux



Asia SLP



Sib SLP



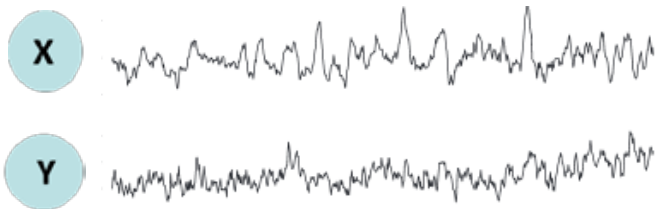
years

Monthly anomalies 1979-2014





# PROBLEMS WITH CROSS-CORRELATION

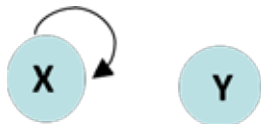


Assume  $X_{t-1}$  and  $Y_t$  correlate strongly:

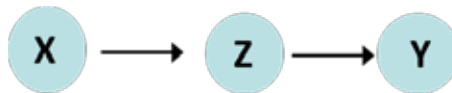
$$\text{e.g. } \rho(X_{t-1}, Y_t) = 0.7$$

Does this mean X causes Y?

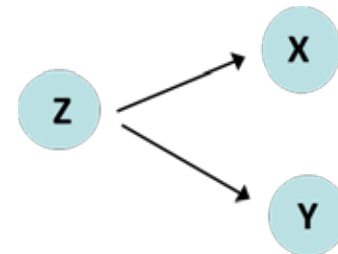
Auto-correlation



Indirect link



Common driver



Multi-variate approach is required

# CAUSAL EFFECT NETWORK (CEN)

## Step 1

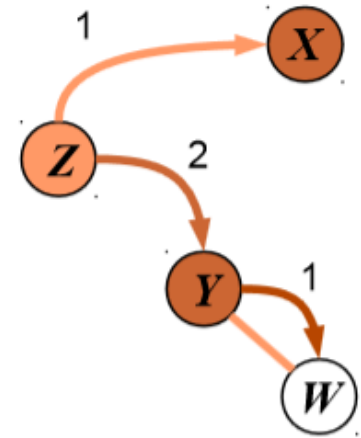
Find causal links

Estimate the parent processes for each actor:  
Exclude spurious correlations due to auto-correlation, common drivers, indirect links

## Step 2

Estimate link strength

Calculate the link strength via multiple linear regression



# STEP 1: CALCULATE THE PARENT PROCESSES FOR PoV

- Which actors are significantly correlated with the PoV index?

$$P_0 = \{v\text{-flux}_{t-1}, \text{PoV}_{t-1}, \text{Ural-SLP}_{t-1}, \text{Ural-SLP}_{t-2}, \text{AO}_{t-1}, \text{EA-snow}_{t-1}\}$$

## Test Hypothesis

Does Eurasian snow cover influence the polar vortex with a lag of one month?

- $\rho(\text{EA-snow}_{t-1}, \text{PoV}_t) = -0.3$  ( $\mathbf{a} < 0.01$ )

- $\rho(\text{EA-snow}_{t-1}, \text{PoV}_t \mid v\text{-flux}_{t-1}) = -0.1$  ( $\mathbf{a} > 0.01$ )

$\rho(X, Y \mid Z)$  = partial correlation of X and Y given Z

- EA-snow and PoV are **conditionally independent**

# STEP 1: CALCULATE THE PARENT PROCESSES FOR PoV

$$P_0 = \{v\text{-flux}_{t-1}, \text{PoV}_{t-1}, \text{Ural-SLP}_{t-1}, \text{Ural-SLP}_{t-2}, \text{AO}_{t-1}, \text{EA-snow}_{t-1}\}$$

$$P_1 = \{v\text{-flux}_{t-1}, \text{PoV}_{t-1}, \text{Ural-SLP}_{t-1}\}$$

## Test Hypothesis

Does poleward heat-flux influence the polar vortex with a lag of one month?

- ▶  $\rho(v\text{-flux}_{t-1}, \text{PoV}_t) = -0.7$  ( $\mathbf{a} < 0.01$ )
- ▶  $\rho(v\text{-flux}_{t-1}, \text{PoV}_t \mid \text{Ural-SLP}_{t-1}) = -0.6$  ( $\mathbf{a} < 0.01$ )
- ▶  $\rho(v\text{-flux}_{t-1}, \text{PoV}_t \mid \text{PoV}_{t-1}) = -0.6$  ( $\mathbf{a} < 0.01$ )
- ▶  $\rho(v\text{-flux}_{t-1}, \text{PoV}_t \mid \text{PoV}_{t-1}, \text{Ural-SLP}_{t-1}) = -0.6$  ( $\mathbf{a} < 0.01$ )
- ▶ v-flux and PoV are **conditionally dependent**

# CEN ALGORITHM

## Step 1

Find causal links

$$\mathcal{P}_0 = \{v\text{-flux}_{t-1}, \text{PoV}_{t-1}, \text{Ural-SLP}_{t-1}, \text{Ural-SLP}_{t-2}, \text{AO}_{t-1}, \text{EA-snow}_{t-1}\}$$

$$\mathcal{P}_1 = \{v\text{-flux}_{t-1}, \text{PoV}_{t-1}, \text{Ural-SLP}_{t-1}\}$$

$$\mathcal{P}_{\text{PoV}} = \{v\text{-flux}_{t-1}, \text{PoV}_{t-1}, \text{Ural-SLP}_{t-1}\}$$

## Step 2

Estimate link strength

Linear regression:

$$\text{PoV}^*_t = \beta_0 + \beta_1 v\text{-flux}^*_{t-1} + \beta_2 \text{Ural-SLP}^*_{t-1} + \beta_3 \text{PoV}^*_{t-1} + \varepsilon$$

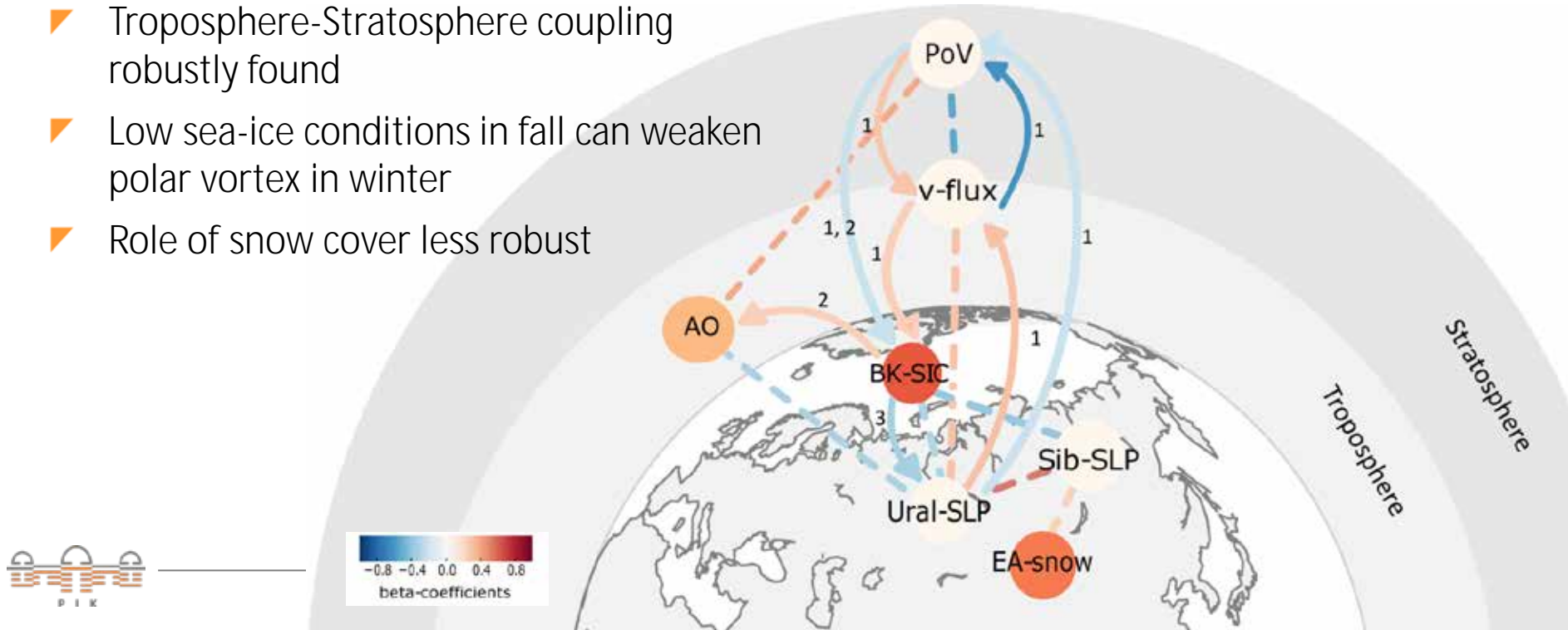
(We account for multiple-testing)

Repeat Step 1+2 for each actor

$$\mathcal{P} = \{\mathcal{P}_{\text{AO}}, \mathcal{P}_{\text{BK-SIC}}, \mathcal{P}_{\text{EA-snow}}, \mathcal{P}_{v\text{-flux}}, \mathcal{P}_{\text{PoV}}, \mathcal{P}_{\text{Sib-SLP}}, \mathcal{P}_{\text{Ural-SLP}}\}$$



# RESULTS: CAUSAL EFFECT NETWORK

- CEN constructed for winter (DJF)
- Troposphere-Stratosphere coupling robustly found
- Low sea-ice conditions in fall can weaken polar vortex in winter
- Role of snow cover less robust



# PART II

## Response-guided causal precursor detection for predictions



**AGU PUBLICATIONS**




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**Geophysical Research Letters**

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**RESEARCH LETTER**  
10.1002/2017GL074696

**Early prediction of extreme stratospheric polar vortex states based on causal precursors**

**Marlene Kretschmer<sup>1,2</sup> , Jakob Runge<sup>3</sup> , and Dim Coumou<sup>1,4</sup> **

<sup>1</sup>Potsdam Institute for Climate Impact Research, Earth System Analysis, Potsdam, Germany, <sup>2</sup>Department of Physics, University of Potsdam, Potsdam, Germany, <sup>3</sup>Imperial College, Grantham Institute, London, UK, <sup>4</sup>Department of Water and Climate Risk, Institute for Environmental Studies (IVM), VU University Amsterdam, Amsterdam, Netherlands

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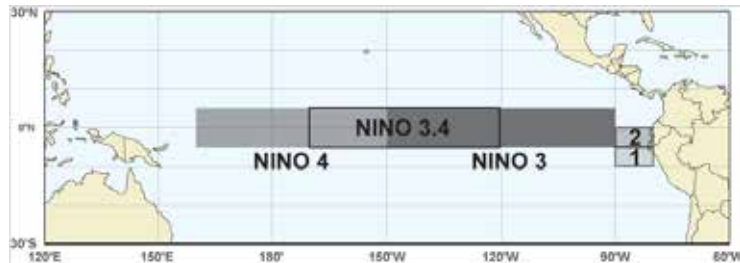
**Abstract** Variability in the stratospheric polar vortex (SPV) can influence the tropospheric circulation and thereby winter weather. Early predictions of extreme SPV states are thus important to improve forecasts of

**Key Points:**

- A new scheme to detect causal precursors useful for empirical predictions is introduced
- Subseasonal causal precursors of the stratospheric polar vortex are identified
- Enables skillful predictions of extremely weak and strong vortex states at long lead times

# MOTIVATION: LIMITATIONS OF CEN

- CEN outcome depends on included actors
- Which processes and hypothesis should be considered?
- Over which regions should the indices be calculated?  
e.g. which ENSO index?



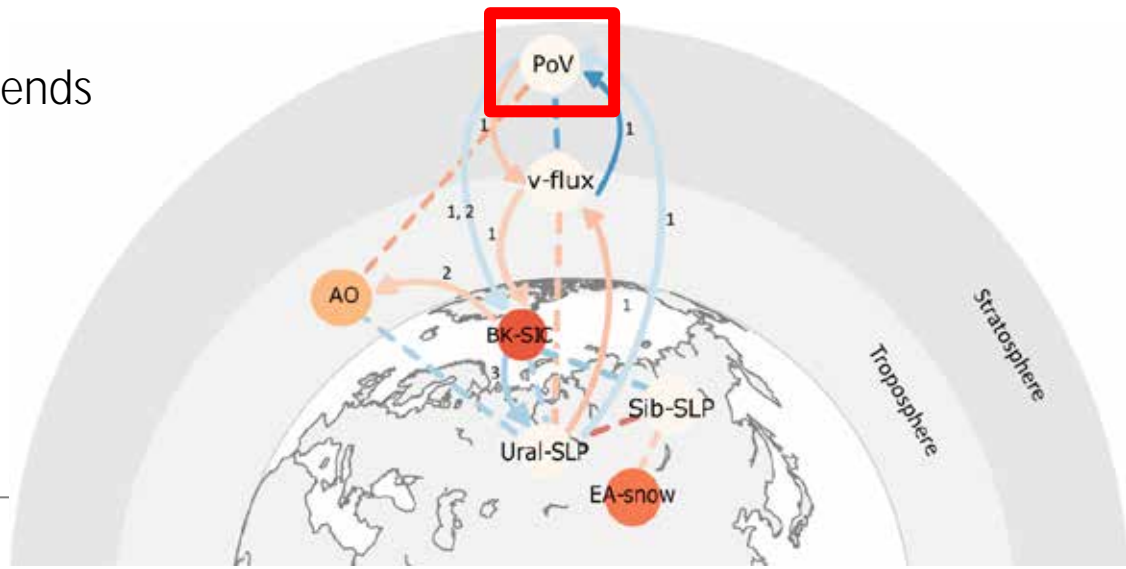
## AIM

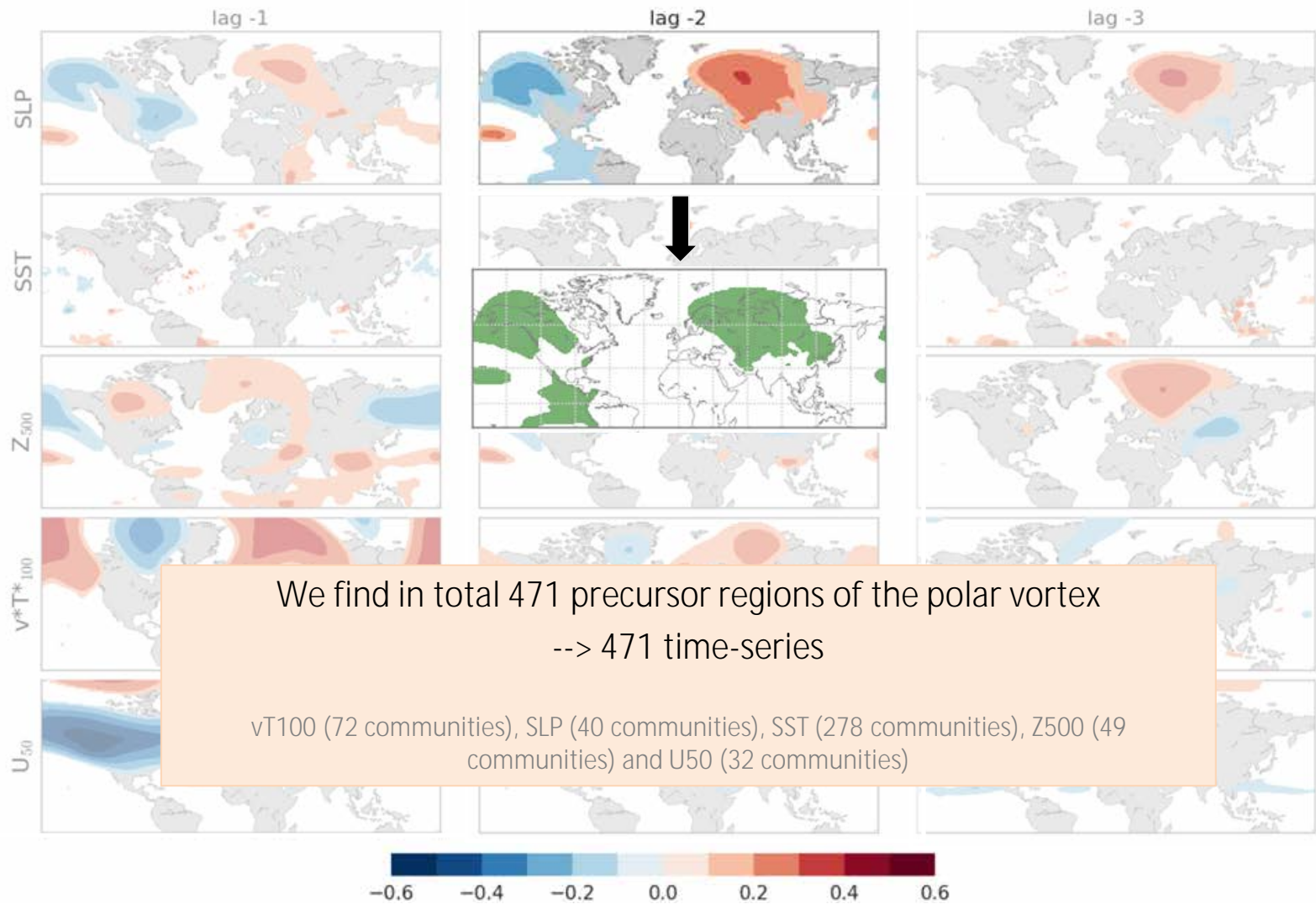
Algorithm that objectively identifies potential drivers of an index of interest



# DATA AND PARAMETER SELECTION

- Response variable:  
Polar Vortex index in winter (NDJFM)
- Potential drivers:  
SST, SLP, GPH 500mb,  $v \cdot T^*$  100mb, uwind 50mb  
from 20°S – 90°N
- Calculate anomalies, remove trends
- Half-monthly time-series
- Maximum lag = 4 months  
(8 time-steps)





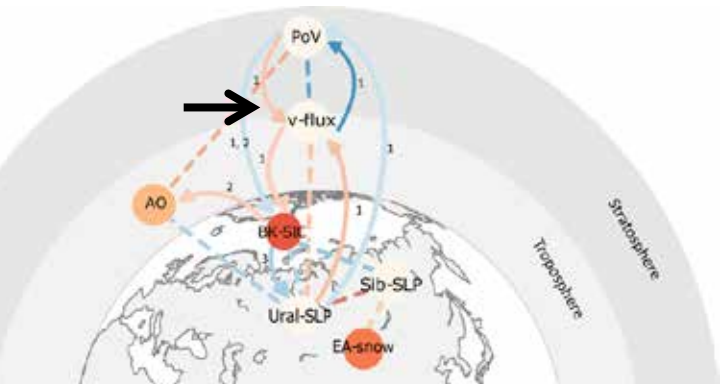
# DETECTION OF CAUSAL DRIVERS

After we apply CEN-algorithm, from the 471 potential drivers only 3 causal precursors remain

Region 1: PoV (lag-1)

Region 2:  $v^*T^*$  at 100hPa (lag-1)

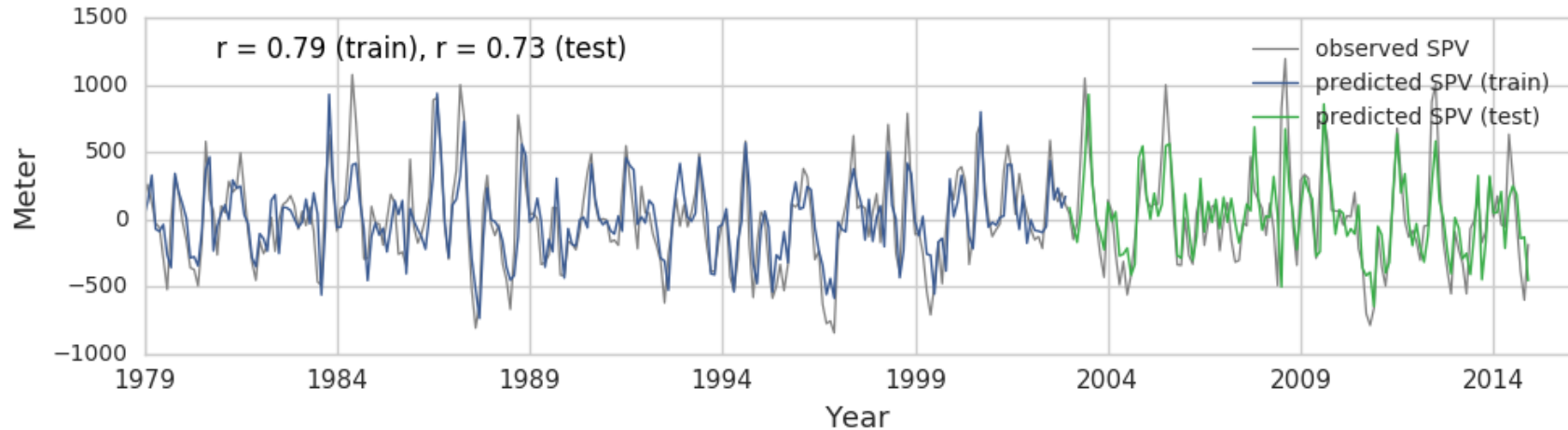
Region 3:  $v^*T^*$  at 100hPa (lag-1)



Linear Regression model:

$$\text{PoV}_t = \beta_0 + \beta_1 \text{PoV}_{t-1} + \beta_2 \text{Region2}_{t-1} + \beta_3 \text{Region3}_{t-1} + \varepsilon$$

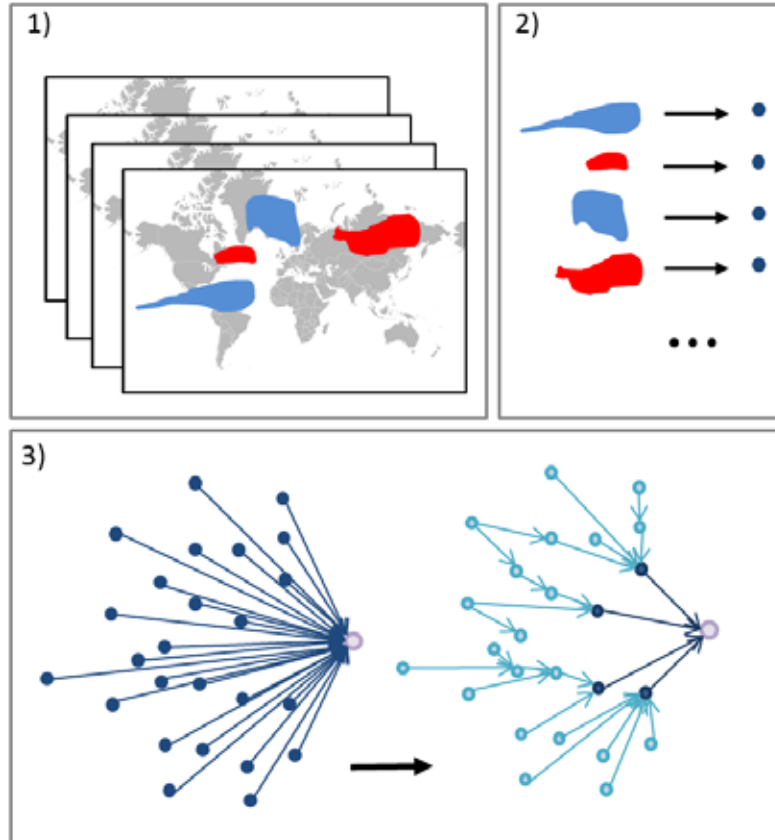
# EVALUATION OF DETECTION SCHEME AND REGRESSION MODEL



Do RG-CPD for training data and apply to independent test data:

- Robust precursors
- No overfitting of model

# RESPONSE-GUIDED CAUSAL PRECURSOR DETECTION (RG-CPD)



1) Detect regions in multi-variate data which correlate positively (red) or negatively (blue) with the response variable at different lags

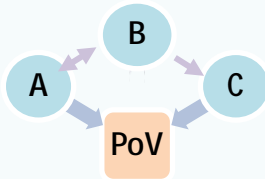
2) Take area-weighted averages of all regions creating time-series of precursors.

3) A causality test removes all non-causal links due to common drivers, auto-correlation or indirect links.

# CONCLUSION

## PART I

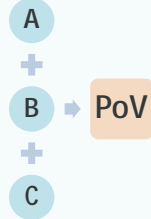
Causal effect networks for hypothesis testing



- Correlation analysis is limited in interpretability
- CEN-algorithm is multi-variate approach to overcome some limitations
- identifies and quantifies causal relationships
- Useful for hypothesis testing

## PART II

Response-guided causal precursor detection for predictions

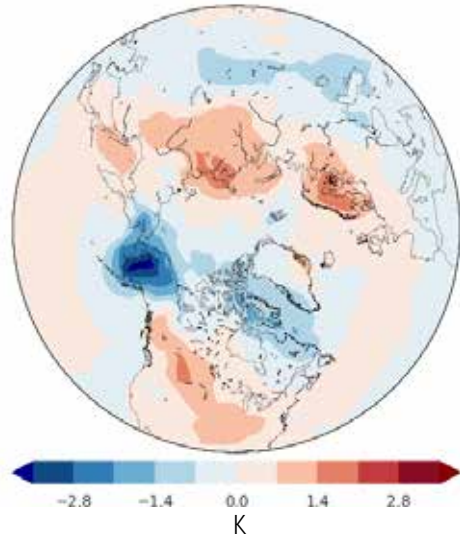


- RG-CPD algorithm objectively detects causal precursors of a response variable
- Avoids overfitting of linear models and is therefore also suitable for predictions
- Restriction to longer lead-times can be used for early-warning systems



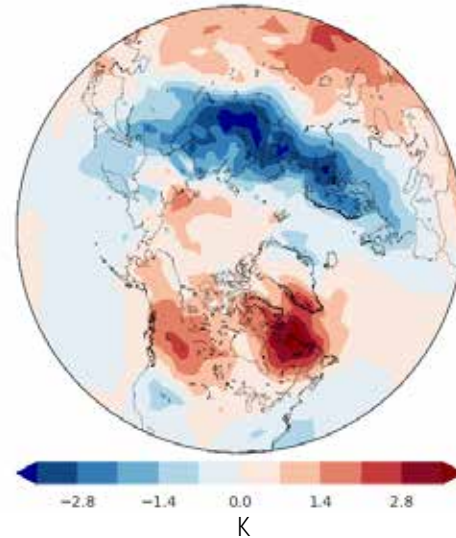
# SURFACE TEMPERATURE RESPONSE

Strong Polar Vortex



Mild winters, +AO

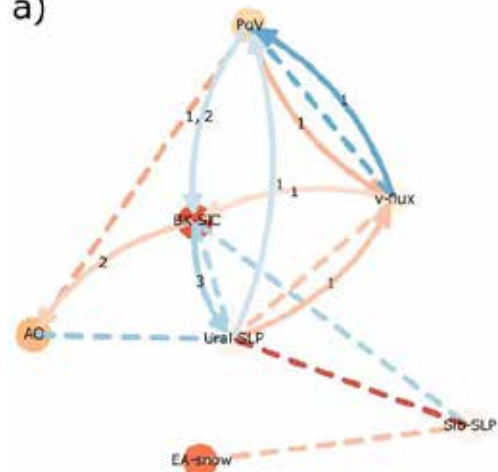
Weak Polar Vortex



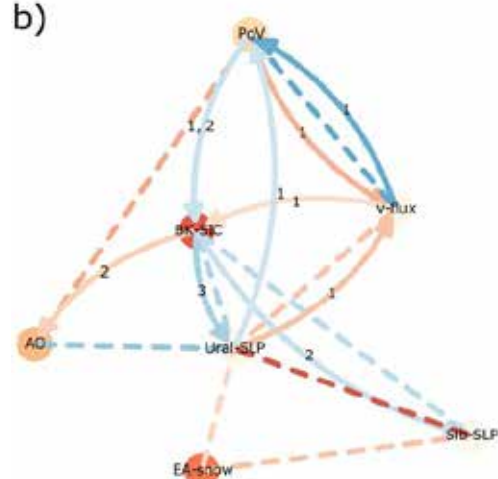
Cold winters, -AO



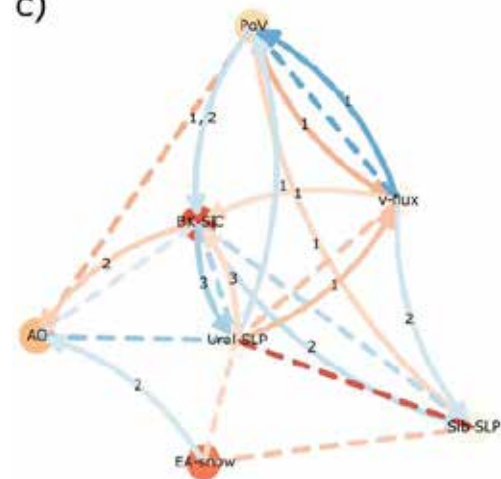
a)



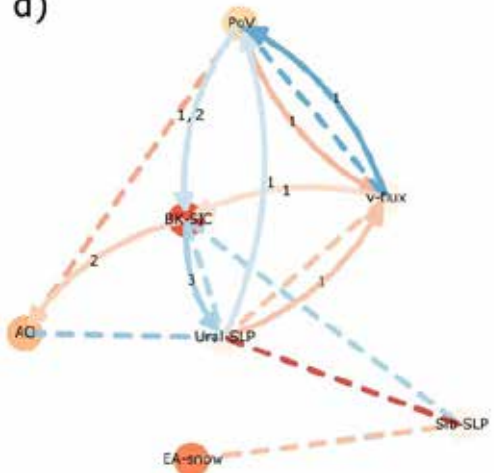
b)



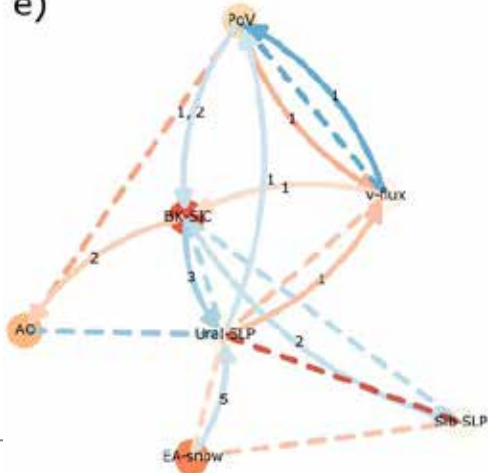
c)



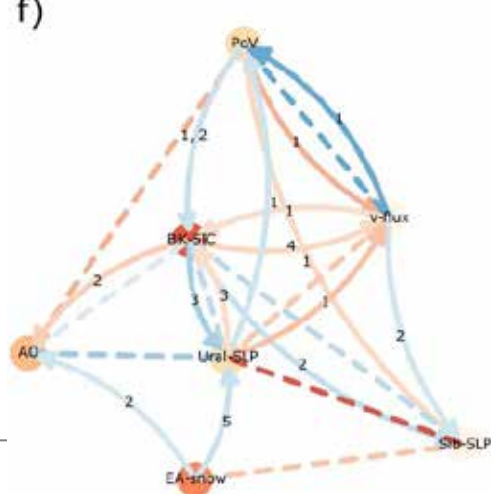
d)



e)

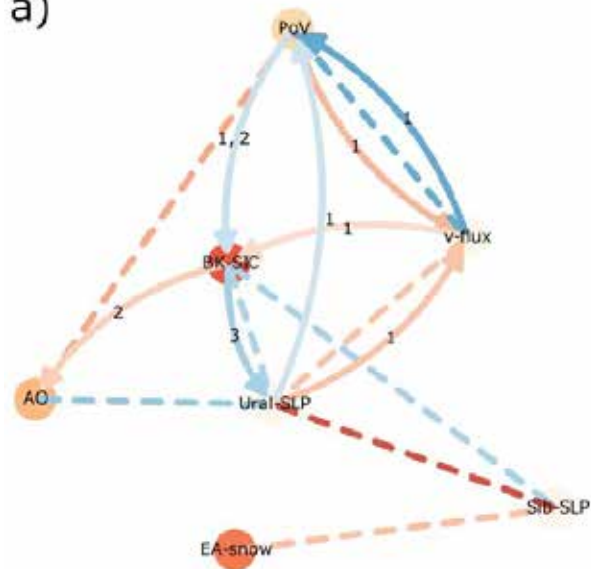


f)



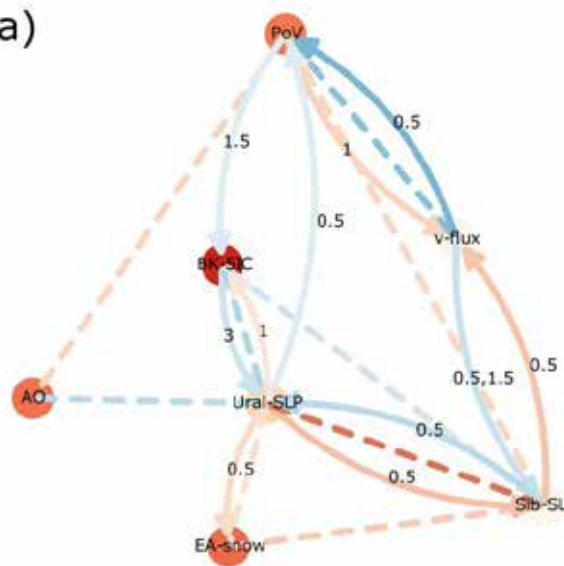
monthly

a)



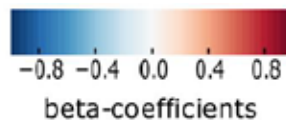
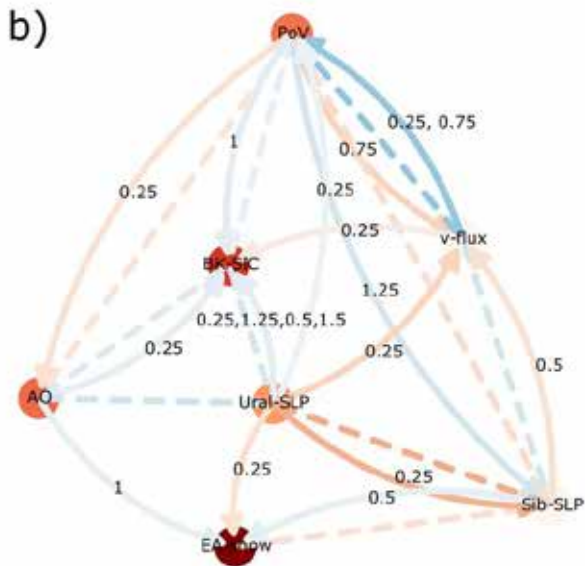
2-weekly

a)



weekly

b)



# LONG LEAD-LAG PREDICTION SKILL

Receiver-operating-characteristic (ROC)  
false-positive-rate vs. true-positive-rate for  
different percentiles

- 64% of weak SPV states are predicted by our model with a false-alarm-rate of ~4% (odds-ratio = 42.3)
- For longer lead-times, models still correctly predict 42% (16-30 days ahead), 22% (31-45 days ahead) and 14% (46-60 days ahead) with associated odds-ratios of 10.3, 3 and 1.5.

